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Effect of fin thickness on the air-side performance of wavy fin-and-tube heat exchangers under dehumidifying conditions

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Abstract

This study investigated the effect of fin thickness on the air-side performance of wavy fin-and-tube heat exchangers under dehumidifying conditions. A total of 10 samples were tested with associated fin thickness (δ_f) of 0.115 mm and 0.25 mm, respectively. For a heat exchanger with two rows (N = 2) and fin pitch F_p of 1.41 mm, the effect of fin thickness on the heat transfer coefficient is more pronounced. The heat transfer coefficients for $\delta_f = 0.25$ mm is about 5–50% higher than those for $\delta_f = 0.115$ mm whereas the pressure drop for $\delta_f = 0.25$ mm is about 5–20% higher. The unexpected difference in heat transfer coefficient subject to fin thickness is attributable to better interactions between the directed main flow and the swirled flow caused by the condensate droplet for $\delta_f = 0.25$ mm. The maximum difference in heat transfer coefficients for N = 2 and $F_p = 2.54$ mm subject to the influence of fin thickness is reduced to about 20%, and there is no difference in heat transfer coefficients diminishes considerably. This is because of the presence of tube row, and the unsteady/ vortex shedding feature at the down stream of wavy channel. Based on the present test results, a correlation is proposed to describe the air-side performance for wavy fin configurations, the mean deviations of the proposed heat transfer and friction correlations are 7.9% and 7.7%, respectively.

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Keywords: Air-side performance; Wavy fin-and-tube heat exchangers; Colburn factor; Friction factor; Dehumidifying conditions

1. Introduction

Plate fin-and-tube heat exchangers are a basic type of heat exchanger employed in many industrial applications such as air conditioning, refrigeration and other thermal processes. In application, the dominated thermal resistance on the air-side of the heat exchanger normally limits the heat transfer rate. One way to enhance the heat transfer on the air-side of the heat exchanger is to modify the fin geometry. Among the enhanced fin configurations, herringbone wavy fin-and-tube heat exchangers are currently widely used because the corrugated fins can provide additional surface area and lengthen the mixing length of the airflow. In their application as evaporators, the surface temperature of the fins is generally below the dew point temperature. As a result, the moist air is condensed on the fins, giving rise to a significant change of the air-side performance of the heat exchanger. Development of the numerical simulation of fin-and-tube heat exchangers is generally difficult due to the complexity of the moist airflow pattern across the heat exchangers, so experimental study is needed.

The air-side performance of wavy fin-and-tube heat exchangers have been studied by a number of researches, see [1-5]. However, the effect of fin thickness on the air-side performance has received little attention in literature [6-8].

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Nomenclature

A_{f}	surface area of fin, m ²	$i_{\rm s,p,i,m}$	saturated air enthalpy at the mean inside tube
A_{\min}	minimum free flow area, m ²		wall temperature, J kg ⁻¹
Ao	total surface area, m ²	<i>i</i> s,p,o,m	saturated air enthalpy at the mean outside tube
$A_{\rm p,i}$	inside surface area of tubes, m ²	-	wall temperature, J kg ⁻¹
$A_{\rm p,o}$	outside surface area of tubes, m ²	<i>i</i> s,w,m	mean saturated air enthalpy at the mean water
$b_{\rm p}$	slope of the air saturation curved between the		film temperature of the fin surface, $J kg^{-1}$
	outside and inside tube wall temperature,	j	Colburn factor
	$J kg^{-1} K^{-1}$	K_0	modified Bessel function solution of the second
$b_{\rm r}$	slope of the air saturation curved at the mean		kind, order 0
	water temperature and the inside wall tempera- ture, $J kg^{-1} K^{-1}$	K_1	modified Bessel function solution of the second kind, order 1
$b_{\rm w.m}$	slope of the air saturation curved at the mean	$K_{\rm c}$	contraction pressure loss coefficient
,	water film temperature of the fin surface,	K _e	expansion pressure loss coefficient
	$J kg^{-1} K^{-1}$	ĸ	thermal conductivity of fin, $W m^{-1} K^{-1}$
$b_{w p}$	slope of the air saturation curved at the mean	k_i	thermal conductivity of water, $W m^{-1} K^{-1}$
,p	water film temperature of the tube surface,	$k_{\rm p}$	thermal conductivity of tube, $W m^{-1} K^{-1}$
	$J kg^{-1} K^{-1}$	k _w	thermal conductivity of water film, $W m^{-1} K^{-1}$
$C_{n,n}$	moist air specific heat at constant pressure.	Ľ	depth of heat exchanger, m
- p,a	$J kg^{-1} K^{-1}$	L_{n}	tube length. m
$C_{n,w}$	water specific heat at constant pressure.	Ň	number of longitudinal tube rows
- <i>p</i> ,w	$J kg^{-1} K^{-1}$	m.	air mass flow rate. kg s^{-1}
D _a	fin collar outside diameter, m	m _w	water mass flow rate, kg s ^{-1}
D:	tube inside diameter, m	ΛP	pressure drop. Pa
D_{a}	tube outside diameter m	P_1	longitudinal tube pitch m
£ 0 f	friction factor	$P_{\rm T}$	transverse tube pitch, m
f;	in-tube friction factor	P_{d}	wave height, m
F	correction factor	Pr	Prandtl number
F.,	fin pitch, mm	Ò,	air-side heat transfer rate. W
$F_{\rm s}^{\rm P}$	fin spacing, mm	\tilde{O}_{avg}	average heat transfer rate. W
Ğmax	mass flux of the air based on minimum free flow	\dot{O}_{w}	water-side heat transfer rate. W
шах	area, kg $m^{-2} s^{-1}$	$\widetilde{R}H_{in}$	inlet relative humidity
$h_{\rm co}$	sensible heat transfer coefficient, $W m^{-2} K^{-1}$	Re_{D_i}	Reynolds number based on inside diameter
$h_{\rm i}$	inside heat transfer coefficient, $W m^{-2} K^{-1}$	Re_{D_c}	Reynolds number based on outside diameter
$h_{0,w}$	total heat transfer coefficient for wet external	c.	(include collar)
-,	fin, $W m^{-2} K^{-1}$	r _i	distance from the center of the tube to the fin
I_0	modified Bessel function solution of the first		base, m
	kind, order 0	ro	distance from the center of the tube to the fin
I_1	modified Bessel function solution of the first		tip, m
	kind, order 1	$T_{\rm a,in}$	inlet air temperature, °C
i _{a,in}	inlet air enthalpy, J kg ⁻¹	$T_{\rm p,i,m}$	mean temperature of the inner tube wall, °C
i _{a,m}	mean air enthalpy, J kg ⁻¹	$T_{\rm p,o,m}$	mean temperature of the outer tube wall, °C
<i>i</i> _{a,out}	outlet air enthalpy, $J kg^{-1}$	$T_{\rm r,m}$	mean temperature of water, °C
<i>i</i> m	mean enthalpy, J kg ⁻¹	$T_{\rm w,in}$	inlet water temperature, °C
<i>i</i> _{r,in}	saturated air enthalpy at the inlet water temper-	$T_{\rm w,out}$	outlet water temperature, °C
	ature, J kg ⁻¹	$U_{\mathrm{o,w}}$	wet surface overall heat transfer coefficient,
<i>i</i> _{r,m}	mean saturated air enthalpy at the mean water		based on enthalpy difference, kg m ^{-2} s ^{-1}
	temperature, J kg ⁻¹	$V_{\rm c}$	maximum velocity across heat exchanger, m s^{-1}
<i>i</i> _{r,out}	saturated air enthalpy at the outlet water tem-	$V_{ m fr}$	frontal velocity, m s^{-1}
	perature, J kg ⁻¹	$\mathcal{Y}_{\mathbf{W}}$	thickness of condensate water film, m
i _{s,fm}	saturated air enthalpy at the fin mean tempera-		
	ture, J kg ^{-1}	Greek s	symbols
i _{s,fb}	saturated air enthalpy at the fin base tempera-	$\delta_{ m f}$	fin thickness, m
	ture, J kg ⁻¹	$\eta_{\rm f,wet}$	wet fin efficiency

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θ	corrugation angle, degree	$ ho_{ m m}$	mean mass density of air, kg m^{-3}
$ ho_{ m i}$	mass density of inlet air, kg m	σ	contraction ratio of cross-sectional area
$ ho_{ m o}$	mass density of outlet air, kg m^{-3}		

Recently, Wongwises and Chokeman [9] studied the effects of fin thickness on the heat transfer and friction characteristics of a fin-and-tube heat exchanger having herringbone wavy fin configuration under dry surface conditions. In contrast to a dry surface, there is no related data reported about the influence of fin thickness on the air-side performance when condensation takes place on the heat transfer surfaces. As a consequence, it is the main objective of this study to investigate the effects of fin thickness on the air-side heat transfer and friction characteristics of herringbone wavy fin-and-tube heat exchangers under dehumidifying conditions. Suitable correlations are also proposed to predict the heat transfer and friction characteristics.

2. Experimental apparatus

The schematic diagram of the experimental air-circuit assembly tunnel is shown in Fig. 1. It consists of a closed-loop wind tunnel in which air is circulated by an axial fan (2.2 kW), varying the air velocity with an inverter ranging 0.5–6 m/s. The air duct is made from galvanized steel sheet and has a 480 mm \times 460 mm cross-section. To obtain a uniform flow into the tested channel, air was forced through a mixture and straightener before entering the test section. The airflow was measured by a nozzle

based on the ASHRAE 41.2 Standard [10] and the pressure drops across the tested heat-exchanger and nozzle were detected by a manometer with uncertainty ± 0.5 Pa. The inlet air temperature and humidity were controlled at approximately 28 °C and 60%, respectively. The inlet/outlet air temperatures across the test section and the inlet/ outlet water temperatures from the tested heat exchanger were measured by T-type thermocouples having an accuracy of ± 0.1 °C. The relative humidity across the tested heat-exchanger was controlled by a ventilation unit. A boiler was used to increase relative humidity. The working fluid in the tube-side of the heat exchanger was chilled water which provided a refrigeration system capacity of up to10.5 kW. The water temperature was kept constant at 7 °C; the water was pumped out of a storage tank, and was passed through a filter, flow meter, test section, and returned to the storage tank. The temperature differences on the water-side were measured by RTD (Pt-100 Ω), with a calibrated accuracy of ± 0.05 °C. The flow rate of the water was kept constant at 0.14 kg/s and detected by a flow meter with a precision of ± 0.01 kg/s.

A total of 10 herringbone wavy fin-and-tube heat exchangers, having various geometric parameters, were tested in this study. The details of the test samples are shown in Table 1. The accuracies of the measurement sensors and



Fig. 1. Schematic diagram of the experimental apparatus.

 Table 1

 Geometric dimensions of the sample wavy fin-and-tube heat exchangers

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No.	D _o (mm)	D _c (mm)	P _T (mm)	P _L (mm)	F _p (mm)	$\delta_{ m f}$ (mm)	Ν
1	9.53	9.76	25.4	19.05	1.41	0.115	2
2	9.53	9.76	25.4	19.05	1.81	0.115	2
3	9.53	9.76	25.4	19.05	2.54	0.115	2
4	9.53	9.76	25.4	19.05	2.54	0.115	4
5	9.53	9.76	25.4	19.05	2.54	0.115	6
6	9.53	10.03	25.4	19.05	1.41	0.250	2
7	9.53	10.03	25.4	19.05	1.81	0.250	2
8	9.53	10.03	25.4	19.05	2.54	0.250	2
9	9.53	10.03	25.4	19.05	2.54	0.250	4
10	9.53	10.03	25.4	19.05	2.54	0.250	6

Notes: Tube layouts of all heat exchangers are staggered layout. Tubes are made of copper with a wall thickness of 0.3 mm.

Table 2

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The	accuracies	ot	the	measurement
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Parameters	Accuracy
Inlet air dry-bulb temperature, $T_{a,in}$	±0.1 °C
Inlet air relative humidity, RH _{in}	$\pm 5\%$
Pressure drop, ΔP	±0.5 Pa
Inlet water temperature, $T_{w,in}$	±0.1 °C
Water flow rate, $\dot{m}_{\rm w}$	± 0.01 kg/s

Table 3

Uncertainties of the derived experimental values

Parameters	Uncertainties (%)
Reynolds number, Re_{D_c}	± 1.0
Air-side heat transfer rate, \dot{Q}_{a}	± 5.5
Water-side heat transfer rate, $\dot{Q}_{\rm w}$	± 6.3
Pressure drop, ΔP	± 0.5
Colburn factor, j	±15.4
Friction factor, f	± 12.3

the uncertainties in derived experimental values are given in Tables 2 and 3. The geometrical parameters can be seen in Fig. 2. The geometric details of the tested herringbone wavy fins are shown in Fig. 3.

3. Data reduction

The following calculations are employed to determine the air-side heat transfer coefficient from the data recorded at steady state conditions during each test run. All fluid properties can be evaluated at the average temperature of the heat exchanger inlet and outlet. The method is based on Wang et al. [7] and Threlkeld [11]. The total rate of heat transfer is averaged from the air-side and water-side as follows:

$$\dot{Q}_{\rm a} = \dot{m}_{\rm a}(i_{\rm a,in} - i_{\rm a,out}) \tag{1}$$

$$\dot{Q}_{\rm w} = \dot{m}_{\rm w} C_{p,\rm w} (T_{\rm w,out} - T_{\rm w,in}) \tag{2}$$

and

$$\dot{Q}_{\rm avg} = (\dot{Q}_{\rm a} + \dot{Q}_{\rm w})/2 \tag{3}$$



Fig. 2. Geometric details of the tested fin-and-tube heat exchangers, and water flow circuit inside the heat exchanger. (Dimension in mm.)

The overall heat transfer coefficient, $U_{o,w}$ which is based on the enthalpy potential can then be determined from

$$\dot{Q}_{\rm avg} = U_{\rm o,w} A_{\rm o} F \Delta i_{\rm m} \tag{4}$$

where A_0 is the total surface area, F is the correction factor for the cross flow unmixed/unmixed configuration, and Δi_m is the mean enthalpy difference for the counter flow,

$$\Delta i_{\rm m} = i_{\rm a,m} - i_{\rm r,m} \tag{5}$$

According to Myers [12], for the counter flow configuration, the mean enthalpy difference is

$$i_{\mathrm{a,m}} = i_{\mathrm{a,in}} + \frac{i_{\mathrm{a,in}} - i_{\mathrm{a,out}}}{\ln \left(\frac{i_{\mathrm{a,in}} - i_{\mathrm{r,out}}}{i_{\mathrm{a,out}} - i_{\mathrm{r,in}}}\right)} - \frac{(i_{\mathrm{a,in}} - i_{\mathrm{a,out}})(i_{\mathrm{a,in}} - i_{\mathrm{r,out}})}{(i_{\mathrm{a,in}} - i_{\mathrm{r,out}}) - (i_{\mathrm{a,out}} - i_{\mathrm{r,in}})}$$
(6)

$$i_{\rm r,m} = i_{\rm r,out} + \frac{i_{\rm r,out} - i_{\rm r,in}}{\ln\left(\frac{i_{\rm a,in} - i_{\rm r,out}}{i_{\rm a,out} - i_{\rm r,in}}\right)} - \frac{(i_{\rm r,out} - i_{\rm r,in})(i_{\rm a,in} - i_{\rm r,out})}{(i_{\rm a,in} - i_{\rm r,out}) - (i_{\rm a,out} - i_{\rm r,in})}$$
(7)

The overall heat transfer coefficient can be written in terms of the total resistance to heat transfer. This total resistance is the sum of the individual resistance as follows:

$$\frac{1}{U_{\text{o,w}}} = \frac{b_{\text{r}}A_{\text{o}}}{h_{\text{i}}A_{\text{p,i}}} + \frac{b_{\text{p}}A_{\text{o}}\ln\left(\frac{D_{\text{c}}}{D_{\text{i}}}\right)}{2\pi k_{\text{p}}L_{\text{p}}} + \frac{1}{h_{\text{o,w}}\left(\frac{A_{\text{p,o}}}{b_{\text{w,p}}A_{\text{o}}} + \frac{A_{\text{f}}\eta_{\text{f,wet}}}{b_{\text{w,m}}A_{\text{o}}}\right)}$$
(8)



Fig. 3. Geometric details of the tested herringbone wavy fins. (Dimension in mm.)

where

$$h_{\mathrm{o,w}} = \frac{1}{\frac{C_{p,a}}{b_{\mathrm{w,m}}h_{\mathrm{co}}} + \frac{y_{\mathrm{w}}}{k_{\mathrm{w}}}} \tag{9}$$

where y_w is the water film thickness. In general practice, the value of y_w/k_w is only 0.5–5% compared to $C_{p,a}/b_{w,m}h_{co}$ [7]. This term is therefore neglected.

The tube-side heat transfer coefficient, (h_i) , is evaluated from the semi-empirical correlation of Gnielinski [13]:

$$h_{\rm i} = \frac{k_i}{D_i} \cdot \frac{(Re_{D_{\rm i}} - 1000)Pr(f_{\rm i}/2)}{1 + 12.7\sqrt{f_{\rm i}/2}(Pr^{2/3} - 1)} \tag{10}$$

where the friction factor is given by

$$f_{\rm i} = \frac{1}{\left(1.58\ln Re_{D_{\rm i}} - 3.28\right)^2} \tag{11}$$

The values of $b_{\rm r}$ and $b_{\rm p}$ can be determined from

$$b_{\rm r} = \frac{(i_{\rm s,p,i,m} - i_{\rm r,m})}{(T_{\rm p,i,m} - T_{\rm r,m})}$$
(12)

$$b_{\rm p} = \frac{(i_{\rm s,p,o,m} - i_{\rm s,p,i,m})}{(T_{\rm p,o,m} - T_{\rm p,i,m})}$$
(13)

The values of $b_{w,p}$ and $b_{w,m}$ are slopes of the saturated enthalpy curve evaluated at the base surface and the fin surface at the outer mean water film temperature. The value of $b_{w,m}$ is determined by trial and error. For the trial and error procedure, the following equation is used to determine $i_{s,w,m}$

$$\begin{split} \dot{i}_{\text{s,w,m}} &= \dot{i}_{\text{a,m}} - \frac{C_{p,\text{a}}h_{\text{o,w}}\eta_{\text{f,wet}}}{b_{\text{w,m}}h_{\text{co}}} \times \left(1 - U_{\text{o,w}}A_{\text{o}}\left[\frac{b_{\text{r}}}{h_{\text{i}}A_{\text{p,i}}} + \frac{b_{\text{p}}\ln\left(\frac{D_{\text{c}}}{D_{\text{i}}}\right)}{2\pi k_{\text{p}}L_{\text{p}}}\right]\right) \\ &\times (i_{\text{a,m}} - i_{\text{r,m}}) \end{split}$$
(14)

The wet fin efficiency, $\eta_{f,wet}$ can be determined based on the Wang [7] method as follows:

$$\eta_{\rm f,wet} = \frac{2r_{\rm i}}{M_{\rm T}(r_{\rm o}^2 - r_{\rm i}^2)} \left[\frac{K_1(M_{\rm T}r_{\rm i})I_1(M_{\rm T}r_{\rm o}) - K_1(M_{\rm T}r_{\rm o})I_1(M_{\rm T}r_{\rm i})}{K_1(M_{\rm T}r_{\rm o})I_0(M_{\rm T}r_{\rm i}) + K_0(M_{\rm T}r_{\rm i})I_1(M_{\rm T}r_{\rm o})} \right] \\ = \frac{i_{\rm a,m} - i_{\rm s,fm}}{i_{\rm a,m} - i_{\rm s,fb}}$$
(15)

where $M_{\rm T} = \sqrt{\frac{2h_{\rm o,w}}{k\delta}}$ and $r_{\rm o} = \sqrt{\frac{P_{\rm T}P_{\rm L}}{\pi}}$.

The air-side heat transfer characteristics are presented in terms of the Colburn j factor

$$j = \frac{h_{\rm c,o}}{G_{\rm max}C_{p,a}}Pr^{2/3}$$
(16)

The flow characteristics determined from the equation proposed by Kays and London [14] termed as the Fanning friction factor. The equation includes the entrance and exit pressure losses:

$$f = \frac{\rho_{\rm m} A_{\rm min}}{\rho_{\rm i} A_{\rm o}} \left[\frac{2\rho_{\rm i} \Delta P}{G_{\rm max}^2} - (1 - \sigma^2 + K_{\rm c}) -2\left(\frac{\rho_{\rm i}}{\rho_{\rm o}} - 1\right) + (1 - \sigma^2 - K_{\rm e})\frac{\rho_{\rm i}}{\rho_{\rm o}} \right]$$
(17)

where $G_{\text{max}} = \rho_{\text{m}} V_{\text{c}}$ and V_{c} is the maximum velocity in the heat exchanger core. σ is the ratio of the minimum free flow area to the frontal area, A_{o} is the total heat transfer area, A_{min} is the minimum free flow area, K_{c} is the core entrance loss coefficient (sudden contraction) and K_{e} is the exit loss (sudden enlargement) coefficient.

4. Results and discussion

The air-side heat transfer and friction characteristics of all tested samples were determined from the experimental data. The thicknesses of the herringbone wavy fins examined in this study were 0.115 and 0.250 mm. The heat transfer coefficient and air-side pressure drop were plotted against the frontal velocity for the tested samples 1 and 6, as shown in Fig. 4. As can be seen in Fig. 4, it was found that the heat transfer coefficient and pressure drop increase with frontal velocity. For Fig. 4(a), the corresponding fin pitch of these two samples is 1.41 mm. Hence, the effective fin spacing for $\delta_f = 0.25$ and $\delta_f = 0.115$ mm is 1.16 mm and 1.3 mm, respectively. The difference between the fin spacing is about 11%. However, it is interested to note that the heat transfer coefficients for $\delta_f = 0.25 \text{ mm}$ are about 5–50% higher than those of $\delta_f = 0.115$ mm whereas the pressure drop of the thick fin is higher than of the thin fin for around 5-20%. The difference is generally increased with the rise of frontal velocities. The surprising differences in heat transfer coefficient between larger and smaller fin thickness are in connection with the drop size and airflow pattern. As indicated by Lin et al. [8,15] who respectively performed a flow visualization of condensate flow patterns along plate surface fin and herringbone fin surface, they reported that the drop size of the condensate is in the range of 0.1–0.5 mm with a corresponding drop height in the range of 0.1-0.7 mm. The presence of condensate is on both sides of the fin. In that regard, the condensate acts not only like a roughness but also a vortex generator. This phenomenon is especially reinforced when the drop size is comparable to the fin spacing. The explanation can be further made clear from the flow visualization experiments conducted by Yoshii et al. [16] who tested a scale-up model of a herringbone fin-and-tube heat exchanger under dehumidifying condition. Yoshii et al. [16] noticed that when the fin channel is close to each other, the condensate which adheres to both sides may cause the airflow within the channel to twist. As a consequence, one can see a dramatic



Fig. 4. Effect of fin thickness on the heat transfer coefficient and pressure drop for 2-row configuration: test results for (a) $F_p = 1.41$ mm and (b) $F_p = 2.54$ mm.

rise of heat transfer coefficient due to the presence of swirled flow when the channel distance is reduced.

For the same number of tube row (N = 2), one can see the associated influence of fin thickness on the heat transfer coefficient is decreased when the fin pitch is increased to 2.54 mm as seen in Fig. 4(b). In fact the maximum difference in heat transfer coefficients subject to the influence of fin thickness is reduced to about 50%, and one can see there is no difference in heat transfer coefficient when the frontal velocity is above 3 m/s. A detailed explanation of the test results will be made in the following paragraph.

A schematic showing the influence of fin thickness in corrugated channels for a smaller and larger fin spacing is shown in Fig. 5. Apparently the airflow may interact with the condensate droplet, giving way to swirled motions. For a larger fin thickness, the corresponding fin spacing is comparatively small. As a consequence, the generated swirled flow may mingle with the main flow and result in a higher heat transfer performance. This phenomenon becomes more pronounced with the frontal velocities which agree well with the trend shown in Fig. 4. Conversely, as shown in Fig. 5b, the interactions between the generated swirled motions and main flow is less prominent at a smaller fin thickness in which the fin spacing is larger. Note that



Fig. 5. Schematic showing the interactions between directed airflow and generated swirled flow for small and large fin spacing: (a) smaller fin spacing and (b) larger fin spacing.

the presented schematic in Fig. 5 also reveals a special characteristic that deserve further attentions. As seen in Fig. 5b, for a larger fin spacing, the main flow may not be effectively directed by the corrugated channel whereas the main flow can flow along the corrugated channel more effectively provided that the fin spacing is less than wave height ($F_s \leq P_d$). This phenomenon had been confirmed by a numerical visualization of the flow pattern within corrugated channels from McNab et al. [17]. Analogous results were also reported by Wang et al. [18] who conducted a flow visualization experiment within enlarged corrugated channels. By examination of the details of the present herringbone fin configurations as shown in Fig. 3, one can see the corresponding wave height is 1.19 mm. As a consequence, for a larger fin thickness of $\delta_f = 0.25$ mm, the relevant fin spacing is 1.13 mm which is smaller than the wave height. This suggests the airflow is effectively directed by the corrugations. In the meantime, at a smaller fin thickness of $\delta_{\rm f} = 0.115$ mm, the associated fin spacing is 1.3 mm that is larger than the wave height. Some part of the airflow is prone to flow across the corrugation without directing by the wave height. As a result, one can see a dramatic difference of heat transfer coefficient between $\delta_f = 0.25$ and $\delta_f = 0.115$ mm. Based on foregoing explanation of the schematic of Fig. 5, one can clearly understand the difference between test results of Fig. 4(a) and (b).

The aforementioned results are applicable for N = 2where corrugations of the wavy channels is comparatively small. With the increase of fin spacing and the number of tube rows, the associated influence of fin thickness on the heat transfer coefficients will be reduced. We will defer this explanations after checking the test results of N = 4 and 6 as shown in Fig. 6. The test results in Fig. 6 clearly substantiate the general arguments made. As seen in Fig. 6(a), despite the heat transfer coefficients for $\delta_{\rm f} = 0.25 \text{ mm}$ are higher than those of $\delta_f = 0.115$ mm for N = 4 and $F_p = 2.54$ mm, the difference is within 15%. Moreover, one can see that there is barely no difference in heat transfer coefficients and pressure drops between $\delta_{\rm f} = 0.25 \, {\rm mm}$ and $\delta_{\rm f} =$ 0.115 mm for N = 6 and $F_p = 2.54$ mm. There are two major explanations about the diminishing influence of fin thickness at a larger fin spacing and at a larger number of tube rows. The first one is related to the influence of tube row. The presence of tube row will certainly alter the airflow



Fig. 6. Effect of fin thickness on the heat transfer coefficient and pressure drops: test results for (a) samples 4 and 9 having 4-row configuration and a fin pitch of 2.54 mm; (b) samples 5 and 10 having 6-row configuration and a fin pitch of 2.54 mm.

path and induces horseshoe vortices [19] that will mix with the main flow. Furthermore, as mentioned in preceding section, the main airflow will interact with the swirled flow caused by the condensate. The presence of tube row will alter the airflow direction, resulting in better flow mixing. The second and most influential reason may be attributed to the nature of wave channels. As can be seen from Ali and Ramadyani [20] who performed a flow visualization experiment in two wavy channels using a dye tracking technique, the fluid flow in the first few corrugations is laminar. However, depending on the Reynolds number, spanwise vortices were shed periodically from certain corrugation at the downstream of a wider channel, but vortex shedding was not observed in narrow channel. Their flow visualization shows considerable flow mixing after several corrugations provided that the fin spacing is large. Wang et al. [18] also observed a unsteady swing at the downstream of a wavy channel that will also promote (or enhance) flow mixing. This apparently agrees with the larger number of tube rows and larger fin spacing of the test results of Fig. 6. In essence, pronounced mixing occurred at a larger fin spacing and at a larger number of tube row, the influence of fin thickness or condensate on the airflow mixing is therefore rather small. Also from Fig. 6, it is also found that the fin thickness has a negligible effect on the friction characteristic when the number of tube rows $N \ge 4$. This is again related to the significant mixing of airflow pattern.

It is obvious from the test results from previous discussions that no single curve can be expected to describe the complex behavior of the present wavy fin for both heat transfer and frictional characteristics. Thus, a multi-regression is carried out to obtain the appropriate correlation form of j and f for the present wavy fin configuration. It is recommended that the following equations are used to describe the present j and f.

$$j = 0.213262 R e_{D_c}^{-0.51507} N^{0.09891} \left(\frac{A_o}{A_{p,o}}\right)^{0.600543} \left(\frac{\delta_f}{P_L}\right)^{0.072448}$$
(18)
$$f = 64.0542 R e_{D_c}^{-0.69284} N^{-0.5237} \left(\frac{A_o}{A_{p,o}}\right)^{-0.54736} \left(\frac{\delta_f}{P_L}\right)^{-0.98371}$$
(19)



Fig. 7. Comparison of the proposed correlations against experimental data: (a) Colburn j factor and (b) friction factor.

As shown in Fig. 7, the proposed heat transfer and friction correlations (Eqs. (18) and (19)) can describe 91.3% and 87.5% of the *j* and *f* factors within $\pm 15\%$, respectively. The mean deviations of the proposed heat transfer and friction correlations are 7.9% and 7.7%, respectively.

5. Conclusions

The present study investigated the effect of fin thickness on the air-side performance of wavy fin-and-tube heat exchangers under dehumidifying conditions. A total of 10 samples were tested with associated fin thickness of 0.115 mm and 0.25 mm, respectively. The following conclusions based on the test results can be made:

1. For N = 2 and $F_p = 1.41$ mm, the effect of fin thickness on the heat transfer coefficient is more pronounced. The heat transfer coefficients for $\delta_f = 0.25$ mm is about 5–50% higher than those for $\delta_f = 0.115$ mm whereas the pressure drop for $\delta_f = 0.25$ mm is about 5–20% higher. The unexpected difference in heat transfer coefficient subject to fin thickness is attributable to better interactions between the directed main flow and the swirled flow caused by the condensate droplet for $\delta_f = 0.25$ mm.

- 2. For N = 2 and $F_p = 2.54$ mm, the associated influence of fin thickness on the heat transfer coefficient is decreased when compared to those of $F_p = 1.41$ mm. The maximum difference in heat transfer coefficients subject to the influence of fin thickness is reduced to approximately 20%, and there is no difference in heat transfer coefficient when the frontal velocity is above 3 m/s.
- 3. For $N \ge 4$ and $F_p = 2.54$ mm, the influence of fin thickness on the heat transfer coefficients diminishes considerably. There is negligible difference for N = 6. This is due to the presence of tube row, and the unsteady/vortex shedding feature at the down stream of wavy channel that lead to a significant mixing. Analogous results about the influence of fin thickness on the pressure drop is also shown.
- 4. Based on the present test results, a correlation is proposed to describe the air-side performance for wavy fin configurations, it is found that 91.3% of the *j* factors and 87.5% of the friction factors within $\pm 15\%$. The mean deviations of the proposed heat transfer and friction correlations are 7.9% and 7.7%, respectively.

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